

Precise measurement of the χ_{c0} resonance parameters and branching fractions of $\chi_{c0,c2} \rightarrow \pi^+ \pi^- / K^+ K^-$ *

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Abstract: By analyzing a $\psi(3686)$ data sample containing $(107.7 \pm 0.6) \times 10^6$ events taken with the BESIII detector at the BEPCII storage ring in 2009, the χ_{c0} resonance parameters are precisely measured using $\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-$ events. The mass of χ_{c0} is determined to be $M(\chi_{c0}) = (3415.63 \pm 0.07 \pm 0.07 \pm 0.07) \text{ MeV}/c^2$, and its full width is $\Gamma(\chi_{c0}) = (12.52 \pm 0.12 \pm 0.13) \text{ MeV}$, where the first uncertainty is statistical, the second systematic, and the third for mass comes from χ_{c2} mass uncertainty. These measurements improve the precision of χ_{c0} mass by a factor of four and width by one order of magnitude over the previous individual measurements, and significantly boost our knowledge about the charmonium spectrum. Together with additional $(345.4 \pm 2.6) \times 10^6$ $\psi(3686)$ data events taken in 2012, the decay branching fractions of $\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-$ are measured as well, with precision improved by a factor of three compared to previous measurements. These χ_{c0} decay branching fractions provide important inputs for the study of glueballs.

Keywords: χ_{c0} , BESIII, charmonium, resonance parameter, branching fraction

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Charmonium, the bound state of charm and anti-charm quarks governed by the strong force, is analogous to the ‘hydrogen atom’ in the study of meson spectro-

scopy [1, 2]. Due to its heavy mass, the velocity of the charm quark is relative slow and therefore the system can be well described by a non-relativistic potential model

[3]. By now, the charmonium spectroscopy below the open-charm threshold is well established [4], and a precise study of them is important and necessary for a stringent test of the theory of the strong interaction, quantum chromodynamics (QCD). The χ_{cJ} (spin $J = 0, 1, 2$) charmonia are P -wave $c\bar{c}$ states split by spin-orbit and tensor forces. At the moment, the χ_{c1} and χ_{c2} masses are precisely measured using a scan approach with $p\bar{p}$ annihilation by the E760 [5] and E835 [6] experiments, and by the LHCb [7] experiment in pp collisions, whereas a precise χ_{c0} mass measurement is relatively marginal, with an uncertainty about five times larger [8, 9] than that of $\chi_{c1,c2}$. Improved precision on the χ_{c0} mass is important for probing the spin structure of the strong force, such as the fine structure splitting $M(^3P_2) - M(^3P_0)$, and the singlet-triplet splitting $M(^1P_1) - M_{\text{cog}}(^3P_J)$, where $M_{\text{cog}}(^3P_J)$ is the center-of-gravity of the triplet. This helps precisely determine the spin-orbit and tensor forces.

We also lack knowledge about the precise width of χ_{c0} [4] compared to its $J = 1, 2$ partners [5–7]. A precise width measurement of χ_{c0} serves as an essential input for studying the χ_{c0} decay, such as the $E1$ transition partial width, light hadron decay width, etc. Furthermore, lattice QCD calculations show an excited scalar glueball candidate with mass in the range of 2.8–3.7 GeV [10–13], and the χ_{c0} might contain a gluonic admixture due to the presence of such a nearby glueball. In this sense, the precise χ_{c0} width provides valuable knowledge to investigate the excited glueball spectrum, which was used to explain the $\gamma^* \rightarrow (c\bar{c})(c\bar{c})$ cross section discrepancy [14] between perturbative QCD calculations [15, 16] and the experimental measurement [17].

The decay of χ_{c0} to light hadrons proceeds predominantly via two-gluon exchanges (color-singlet) [18]. The decay widths of the simplest pseudo-scalar final state $\pi^+\pi^-$ and K^+K^- are expected to be identical within SU(3) flavor symmetry. This simple feature also applies to other 0^{++} systems, such as the light glueball candidates $f_0(1500)$ and $f_0(1710)$ [4]. However, the couplings of $f_0(1710)$ to the $\pi^+\pi^-$ and K^+K^- final states differ significantly [19, 20] due to a so-called 'Chiral Suppression' effect [21, 22]. Therefore, a precise measurement of the branching fraction (BF) $\chi_{c0} \rightarrow \pi^+\pi^-/K^+K^-$, together with its full width, provides an ideal testing ground for the study of decays of the glueball candidates. In addition, the color-octet component also plays an important role in charmonium decays, and these precise BF measurements can help to constrain the non-perturbative parameters in QCD calculations [18, 23, 24] and to allow us to finally understand the decay dynamics of charmonium states.

In this Letter, a precise mass and width measurement of χ_{c0} is achieved via $\chi_{c0} \rightarrow \pi^+\pi^-/K^+K^-$ decays. The decay BFs of $\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-$ are precisely measured as well. The analysis is performed using a $\psi(3686)$ data sample consisting of $(107.7 \pm 0.6) \times 10^6$ events taken in

2009 and $(345.4 \pm 2.6) \times 10^6$ events taken in 2012 [25] at BESIII. The $\chi_{c0,c2}$ states are produced copiously in the radiative transition $\psi(3686) \rightarrow \gamma\chi_{c0,c2}$.

The BESIII detector is described in detail elsewhere [26]. Simulated Monte Carlo (MC) samples produced with a GEANT4-based [27] MC simulation software package, which includes the geometric description of the detector as well as its response, are used to determine detection efficiencies, optimize the selection criteria, and estimate background contributions. Signal MC samples of $\psi(3686) \rightarrow \gamma\chi_{c0,c2} \rightarrow \gamma\pi^+\pi^-/\gamma K^+K^-$ are produced. Each channel contains 400,000 signal events. In the simulation, the $\psi(3686)$ resonance is generated with KKMC [28, 29], which includes initial-state-radiation and the beam energy spread. The decays of $\psi(3686) \rightarrow \gamma\chi_{c0,c2} \rightarrow \gamma\pi^+\pi^-/\gamma K^+K^-$ are simulated with the angular distribution taken into account using a previous multipole amplitude measurement by BESIII [30].

To investigate the potential background, an inclusive MC sample containing the same number of $\psi(3686)$ events as data is simulated. This sample includes the production of the $\psi(3686)$ resonance, the ISR production of the J/ψ , and the continuum processes incorporated in KKMC [28, 29]. All particle decays are modeled with EVTGEN [31, 32] using BFs either taken from the Particle Data Group (PDG) [4], when available, or otherwise modeled with LUNDCHARM [33, 34] for all remaining unknown charmonium decays. Final state radiation (FSR) from charged final state particles is incorporated using the PHOTOS package [35]. Di-muon and Bhabha MC samples, each containing one million events, are generated with the Babayaga generator [36] for further background studies.

For the $\psi(3686) \rightarrow \gamma\chi_{c0,c2} \rightarrow \gamma\pi^+\pi^-/\gamma K^+K^-$ signal events of interest, the final states have two high-momentum charged tracks and an energetic radiative photon, with an energy of 261 (128) MeV in the χ_{c0} (χ_{c2}) case, due to the large mass gap between $\psi(3686)$ and $\chi_{c0,c2}$. Charged tracks detected in the multi-layer drift chamber (MDC) are required to be within the polar angle range $|\cos\theta| < 0.93$, where θ is defined with respect to the z axis, which is the symmetry axis of the MDC. For each good charged track, the distance of closest approach to the interaction point (IP) must be less than 10 cm along the z axis, and less than 1 cm in the transverse plane. A candidate event is required to have two good charged tracks with zero net charge.

Photon candidates are identified using isolated showers in the electromagnetic calorimeter (EMC). The deposited energy of each shower must be more than 25 MeV in the barrel region ($|\cos\theta| < 0.80$) and more than 50 MeV in the end-cap region ($0.86 < |\cos\theta| < 0.92$). To exclude showers that originate from charged tracks, the angle subtended by the EMC shower and the position of the closest charged track at the EMC must be greater than

10 degrees as measured from the IP. To suppress electronic noise and showers unrelated to the event, the difference between the EMC time and the event start time is required to be within $[0, 700]$ ns. At least one good photon candidate is required in an event.

To improve the momentum resolution of final state particles and further suppress background, a four-constraint (4C) kinematic fit which constrains the four-momentum of two charged tracks and a photon to the initial $\psi(3686)$ four-momentum is performed. The two charged tracks are assumed to be either $\pi^+\pi^-$ or K^+K^- , and the corresponding kinematic fit chi-squares ($\chi^2_{\gamma\pi^+\pi^-}$ and $\chi^2_{\gamma K^+K^-}$) are obtained. An event is assigned as $\gamma\pi^+\pi^-$ if $\chi^2_{\gamma\pi^+\pi^-} < \chi^2_{\gamma K^+K^-}$, otherwise as γK^+K^- . The radiative photon candidate is selected as the one that yields the smallest χ^2 from the 4C kinematic fit if there are multiple photon candidates within one event. The χ^2 of the kinematic fit is further required to be less than 60 for $\gamma\pi^+\pi^-$ events and 56 for γK^+K^- events, which are optimized by maximizing the Figure-of-Merit $S/\sqrt{(S+B)}$, where S represents the number of normalized events from signal MC samples according to BFs from the PDG [4], and B is the total number of normalized background events estimated from the inclusive, Bhabha and di-muon MC samples.

For $\gamma\pi^+\pi^-$ events, there are radiative Bhabha and $\psi(3686) \rightarrow (\gamma)e^+e^-$ backgrounds. To remove these electrons, the deposited energy of each charged track in the EMC is required to be less than 1.34 GeV. Electrons passing through the EMC gap ($0.81 < |\cos\theta| < 0.86$), which has no crystals between the barrel and end-cap regions, can further survive. To remove these remaining electrons, the dE/dx of a charged particle measured by the MDC is used. For charged tracks falling into the gap region, the $|\chi_{dE/dx}(\pi)|$ [26] is required to be less than 2, where $\chi_{dE/dx}(\pi)$ is the pull value of dE/dx based on the pion hypothesis. The most significant background comes from radiative di-muon and $\psi(3686) \rightarrow (\gamma)\mu^+\mu^-$ events due to serious π and μ mis-identification. These non-peaking background processes are precisely known [4] and can be well simulated at BESIII.

For γK^+K^- events, the background level is much lower due to the higher kaon mass. There are some remaining backgrounds from radiative Bhabha, $\psi(3686) \rightarrow (\gamma)e^+e^-$, and $\psi(3686) \rightarrow \pi^0\pi^0 J/\psi \rightarrow \pi^0\pi^0 e^+e^-$, which are effectively vetoed by requiring the deposited energy of both kaons in the EMC to be less than 1.34 GeV. Since no particle identification is applied to high momentum pions and kaons, there is cross-contamination between $\gamma\pi^+\pi^-$ and γK^+K^- events. According to MC simulation studies, the cross-contamination ratio is small ($< 1\%$). For γK^+K^- events, the background contribution from $\gamma\pi^+\pi^-$ cross-contamination is fixed via MC simulation, and vice versa.

After applying the event selection criteria mentioned

above, the obtained $M(\pi^+\pi^-)$ and $M(K^+K^-)$ invariant mass distributions from data are shown in Fig. 1, where significant numbers of $\chi_{c0,c2}$ signal events are observed. To measure the mass and width of χ_{c0} , as well as the BFs of $\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-$, an unbinned maximum likelihood fit is performed to the $\gamma\pi^+\pi^-$ and γK^+K^- data events simultaneously. In the fit, the BFs of $\chi_{c0,c2} \rightarrow \pi^+\pi^-$ and $\chi_{c0,c2} \rightarrow K^+K^-$ are shared as common parameters between data taken in different years. To avoid using the absolute momentum scale, and therefore significantly improve the mass precision of χ_{c0} , the mass split between χ_{c2} and χ_{c0} , $\Delta M_{20} \equiv M(\chi_{c2}) - M(\chi_{c0})$, is measured instead. Even in this case, the quality of the 2012 data is not as good as the 2009 data due to the worse MDC inner chamber performance during data taking [37], which bring in considerable systematic effects from discrepancies between data and MC simulation. Therefore, only the 2009 data are used for mass and width measurements, *i.e.* ΔM_{20} and the full width Γ of χ_{c0} are shared as common parameters in $\gamma\pi^+\pi^-$ and γK^+K^- data events taken in 2009.

The signal probability-density-function (PDF) is parameterized as

$$[\text{BW}^2(\sqrt{s}) \times \mathcal{P}S_1^2(\sqrt{s}) \times \mathcal{D}^2(\sqrt{s}) \times \mathcal{P}S_2^2(\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-) \times \epsilon(\sqrt{s})] \otimes \text{Resolution}, \quad (1)$$

where $\text{BW}(\sqrt{s})$ is a relativistic Breit-Wigner (BW) amp-

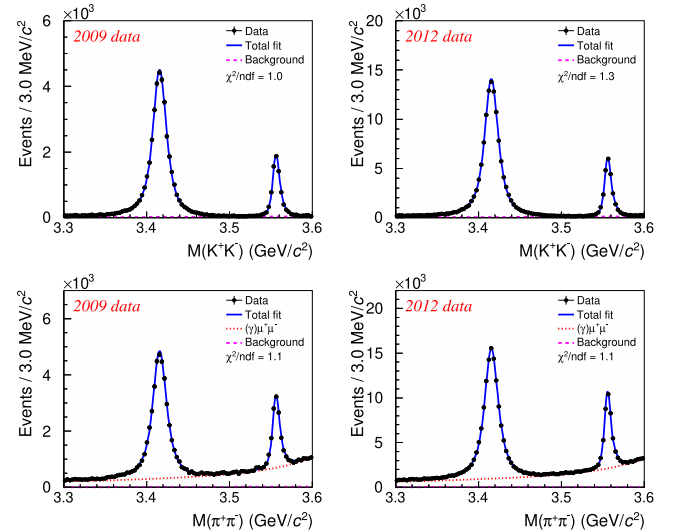


Fig. 1. (color online) The K^+K^- (top row) and $\pi^+\pi^-$ (bottom row) invariant mass distributions from $\psi(3686)$ data taken in 2009 (first column) and 2012 (second column) with fit results overlaid. The black dots with error bars are data, the blue solid curves represent the total fit results, the red dotted lines in bottom panels represent the background component from $(\gamma)\mu^+\mu^-$, and the pink dashed lines represent all other background components.

litude defined as

$$\text{BW}(\sqrt{s}) = \frac{1}{s - M^2 + iM\Gamma \frac{p}{p'} \frac{M}{\sqrt{s}}}, \quad (2)$$

where $\sqrt{s}$ is the $\pi^+\pi^-/K^+K^-$ invariant mass, while M and Γ are the mass and constant width of $\chi_{c0,c2}$, respectively, and p (p') is the momentum of daughter particles in the rest frame of the mother particle with mass $\sqrt{s}$ (M). In the $E1$ radiative transition $\psi(3686) \rightarrow \gamma\chi_{c0,c2}$, the decay width is proportional to a phase space factor $\mathcal{PS}_1(\sqrt{s})$ [38, 39] defined as

$$\mathcal{PS}_1(\sqrt{s}) = \left(\frac{E_\gamma}{E_\gamma^0} \right)^{3/2}, \quad (3)$$

where E_γ is the radiative photon energy and E_γ^0 corresponds to the photon energy at the $\chi_{c0,c2}$ mass M . An additional damping factor $\mathcal{D}(\sqrt{s}) = \left(\frac{(E_\gamma^0)^2}{E_\gamma E_\gamma^0 + (E_\gamma^0 - E_\gamma)^2} \right)^{1/2}$ [40] is also introduced to suppress the higher energy tail. $\mathcal{PS}_2(\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-)$ is the phase space factor of $\chi_{c0,c2}$ decaying into $\pi^+\pi^-/K^+K^-$ [4]. The signal PDF is corrected by a mass-dependent efficiency curve $\epsilon(\sqrt{s})$, which is obtained by MC simulation studies and varies within 1% for the interested mass region, thus parameterized as a linear function. The $\chi_{c0,c2}$ resonance line shapes are further convolved with Gaussian functions to account for the detector resolution. In the fit, the χ_{c2} width is fixed to the known value [4], and the resolution difference between data and MC simulation measured from χ_{c2} data events is used to calibrate that for χ_{c0} .

The shapes of dominant background sources are described by polynomial functions. For γK^+K^- events, the background is low and parameterized as a free second-order polynomial. The small cross-contamination contribution from $\gamma\pi^+\pi^-$ events is fixed via MC simulation. For $\gamma\pi^+\pi^-$ events, the dominating $(\gamma)\mu^+\mu^-$ background is represented by a fourth-order polynomial, which is fixed according to normalized MC events for $\psi(3686) \rightarrow (\gamma)\mu^+\mu^-$ and di-muon processes. Other extra backgrounds with a small contribution ($\sim 3\%$ of the total background) are parameterized as a free second-order polynomial.

Figure 1 shows the fit results. The mass split between χ_{c2} and χ_{c0} is measured to be $\Delta M_{20} \equiv M(\chi_{c2}) - M(\chi_{c0}) = (140.54 \pm 0.07) \text{ MeV}/c^2$. Taking the world average mass $M(\chi_{c2}) = (3556.17 \pm 0.07) \text{ MeV}/c^2$ [4] as input, the χ_{c0} mass is calculated to be $M(\chi_{c0}) = (3415.63 \pm 0.07) \text{ MeV}/c^2$. The width of χ_{c0} is measured to be $\Gamma(\chi_{c0}) = (12.52 \pm 0.12) \text{ MeV}$. The uncertainties here are statistical only.

The systematic uncertainties in the mass split and χ_{c0} width measurements mainly come from the signal and

background PDF shapes as well as the damping factor, momentum-dependent scale, and possible interference effect. In the nominal fit model, a BW function with a mass-dependent width, *i.e.* Eq. (2), is used to describe the $\chi_{c0,c2}$ state. An alternative shape with a constant width BW function is investigated. The difference with respect to the nominal measurement for ΔM_{20} is $0.04 \text{ MeV}/c^2$ and for the χ_{c0} full width $\Gamma(\chi_{c0})$ is 0.08 MeV , which are taken as systematic uncertainties. A damping factor also appears in the signal PDF. We take another form $\mathcal{D}(\sqrt{s}) = e^{-E_\gamma^2/(8\beta^2)}$, where $\beta = 65.0 \pm 2.5 \text{ MeV}$ from the CLEO-c Collaboration [41]. The difference on the measurements of ΔM_{20} and $\Gamma(\chi_{c0})$ is $0.01 \text{ MeV}/c^2$ and 0.01 MeV , respectively.

The uncertainty due to background in the fit is studied in several aspects. The free background components are described by second-order polynomials for both $\gamma\pi^+\pi^-$ and γK^+K^- events. Changing this component to a third-order polynomial either for $\gamma\pi^+\pi^-$ or γK^+K^- events yields differences on the measurements, which are $0.02 \text{ MeV}/c^2$ for ΔM_{20} and 0.04 MeV for $\Gamma(\chi_{c0})$. Interference between $\chi_{c0,c2}$ resonances and continuum is observed in low-mass regions [42], and we account for this by adding the continuum component coherently to the signal PDF. The resulting difference for ΔM_{20} is $0.01 \text{ MeV}/c^2$ and $\Gamma(\chi_{c0})$ is 0.08 MeV . For $\gamma\pi^+\pi^-$ events, the dominant background comes from $(\gamma)\mu^+\mu^-$. Varying the output cross section from Babayaga [36] by $\pm 1\sigma$ for MC simulated background normalization yields a difference of $0.02 \text{ MeV}/c^2$ for ΔM_{20} and 0.02 MeV for $\Gamma(\chi_{c0})$. The shape parameters of this background component are also varied within $\pm 1\sigma$, which yields a difference of $0.01 \text{ MeV}/c^2$ for ΔM_{20} and 0.02 MeV for $\Gamma(\chi_{c0})$. The momentum-dependent scale is simulated by MC. The systematic uncertainty due to the difference between data and MC is studied by correcting the MC distribution of final-state particle momenta to data with χ_{c2} events, which yields a variation of $0.04 \text{ MeV}/c^2$ for ΔM_{20} and 0.01 MeV for $\Gamma(\chi_{c0})$.

Table 1 summarizes all these sources and their corresponding contributions. Assuming all the sources are independent, the total systematic uncertainty is obtained by adding each individual source in quadrature, which is $0.07 \text{ MeV}/c^2$ for ΔM_{20} and 0.13 MeV for $\Gamma(\chi_{c0})$.

The BF of $\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-$ is calculated as

$$\mathcal{B} = \frac{N_{\text{sig}}}{N_{\text{tot}}[\psi(3686)]\epsilon\mathcal{B}[\psi(3686) \rightarrow \gamma\chi_{c0,c2}]}, \quad (4)$$

where N_{sig} is the number of observed $\chi_{c0,c2}$ signal events from the fit, $N_{\text{tot}}[\psi(3686)]$ is the total number of collected $\psi(3686)$ events [25], ϵ is the detection efficiency of $\gamma\pi^+\pi^-/\gamma K^+K^-$ events, and $\mathcal{B}[\psi(3686) \rightarrow \gamma\chi_{c0,c2}]$ is the BF of the $E1$ radiative transition [4]. In practice, a simultaneous fit is performed and the BFs are shared between dif-

Table 1. Sources of systematic uncertainties and their contributions to ΔM_{20} and $\Gamma(\chi_{c0})$ measurements.

Source	$\Delta M_{20} / (\text{MeV}/c^2)$	$\Gamma(\chi_{c0}) / \text{MeV}$
Signal shape	0.04	0.08
Damping factor	0.01	0.01
Polynomial background	0.02	0.04
Interference effect	0.01	0.08
Number of $(\gamma)\mu^+\mu^-$ background	0.02	0.02
Shape of $(\gamma)\mu^+\mu^-$ background	0.01	0.02
Momentum dependent scale	0.04	0.01
Total	0.07	0.13

ferent data sets. The BF's are measured to be $\mathcal{B}(\chi_{c0} \rightarrow K^+K^-) = (6.36 \pm 0.02) \times 10^{-3}$, $\mathcal{B}(\chi_{c0} \rightarrow \pi^+\pi^-) = (6.06 \pm 0.02) \times 10^{-3}$, $\mathcal{B}(\chi_{c2} \rightarrow K^+K^-) = (1.22 \pm 0.01) \times 10^{-3}$, and $\mathcal{B}(\chi_{c2} \rightarrow \pi^+\pi^-) = (1.61 \pm 0.01) \times 10^{-3}$, respectively, where all the uncertainties are statistical only. Table 2 lists the detection efficiencies for each data set.

The systematic uncertainties in the BF measurements mainly come from the total number of $\psi(3686)$ events, detection efficiencies, signal and background PDF shapes, possible interference effect, fit range, 4C kinematic fit, and intermediate BF's.

The total number of $\psi(3686)$ events is measured by counting inclusive hadronic events, with an uncertainty of 0.7% [25]. Detection efficiencies include tracking, photon detection, decay angular distributions, and selection criteria. The uncertainty of photon detection is measured to be 0.5% per photon by studying the $e^+e^- \rightarrow \gamma\mu^+\mu^-$ process and 0.5% is assigned for this analysis. Pion and kaon tracks have a momentum above 1 GeV. The tracking efficiency of such tracks is above 99% at BESIII, by studying $e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$ and $J/\psi \rightarrow K^*K$ events. According to the two-dimensional (2D, p_t vs. $\cos\theta$) tracking efficiencies of data and MC simulation, the uncertainty in each bin is obtained. The final uncertainty due to tracking is estimated as a weighted average over 2D bins.

Decay angular distributions also affect the detection efficiencies. Considering the helicity amplitudes and correlation coefficients measured by BESIII [30], 100 sets of two correlated helicity amplitude parameters are obtained via a 2D sampling. The resulting changes in detection efficiencies, and therefore the corresponding changes of BF's from the simultaneous fit, are taken as systematic uncertainties. The uncertainties due to the pion/kaon EMC deposit energy requirement and fit range are studied using a Barlow test [43], by changing a series of EMC deposit energies and fit ranges. All the alternative choices give results within 1σ of the nominal result, which means these two sources can be ignored.

For the 4C kinematic fit, a correction of the pull distribution of charged track parameters is applied to the MC

Table 2. The detection efficiencies for $\gamma\pi^+\pi^-$ and γK^+K^- data events taken in different years.

	$\epsilon(\gamma\pi^+\pi^-)$	$\epsilon(\gamma K^+K^-)$
2009 χ_{c0}	0.644 ± 0.001	0.589 ± 0.001
2009 χ_{c2}	0.667 ± 0.001	0.624 ± 0.001
2012 χ_{c0}	0.634 ± 0.001	0.577 ± 0.001
2012 χ_{c2}	0.658 ± 0.001	0.613 ± 0.001

Table 3. Sources of systematic uncertainties and their contributions (in %) to BF measurements. "..." means a non-applicable option.

Source	$\gamma\pi^+\pi^-$		γK^+K^-	
	χ_{c0}	χ_{c2}	χ_{c0}	χ_{c2}
$N_{\text{tot}}[\psi(2S)]$	0.7	0.7	0.7	0.7
Tracking	0.1	0.1	0.2	0.1
Photon	0.5	0.5	0.5	0.5
Polynomial background	0.6	0.2	0.1	0.1
Interference effect	0.4	0.0	0.4	0.0
Number of $(\gamma)\mu^+\mu^-$ background	0.1	0.4	0.1	0.1
Shape of $(\gamma)\mu^+\mu^-$ background	0.2	0.1	0.1	0.1
Cross contamination	0.0	0.0	0.0	0.1
Damping factor	0.1	0.2	0.1	0.1
Signal shape	0.1	0.2	0.1	0.1
Angular distribution	...	0.1	...	0.0
4C kinematic fit	0.3	0.2	0.7	0.8
Sum	1.2	1.1	1.2	1.2
Intermediate BF	2.1	2.1	2.1	2.1
Total	2.4	2.4	2.4	2.4

simulation [44]. The uncertainties are taken as half of the efficiency difference with or without helix parameter corrections. The uncertainties on the BF's for $\psi(3686) \rightarrow \gamma\chi_{c0}$ (2.1%) and $\psi(3686) \rightarrow \gamma\chi_{c2}$ (2.1%) are taken from the PDG [4]. The uncertainties due to the signal shape, damping factor and background are studied using the same method as the mass split and width measurement. The cross-contaminations between $\gamma\pi^+\pi^-$ and γK^+K^- events are studied via MC simulations, with input BF's updated by this measurement. The fluctuations due to BF's are taken as systematic uncertainties.

Table 3 summarizes all these sources and their contributions to the BF measurements. Assuming all the sources are independent, the total systematic uncertainties are obtained by adding them in quadrature. The largest systematic uncertainty comes from the intermediate BF's, and all other sources contribute about 1.2%.

In summary, a precise measurement of the χ_{c0} resonance parameters and the $\chi_{c0,c2} \rightarrow \pi^+\pi^-/K^+K^-$ decay BF's is

performed at BESIII by analyzing $\psi(3686)$ data events. The mass split between χ_{c2} and χ_{c0} is measured to be $\Delta M_{20} = (140.54 \pm 0.07 \pm 0.07) \text{ MeV}/c^2$. Taking the χ_{c2} world average mass as input, the χ_{c0} mass is determined to be $M(\chi_{c0}) = (3415.63 \pm 0.07 \pm 0.07 \pm 0.07) \text{ MeV}/c^2$, where the first uncertainty is statistical, the second systematic, and the third from the χ_{c2} mass uncertainty. This is the most precise χ_{c0} mass measurement to date. It is a bit higher ($1.42 \pm 0.49 \text{ MeV}/c^2$) than the BES measurement [8], while it agrees well with the E835 measurement [9]. Our measurement improves the precision of the χ_{c0} mass over previous individual measurements by a factor of four [8, 9]. The full width of χ_{c0} is measured to be $\Gamma(\chi_{c0}) = (12.52 \pm 0.12 \pm 0.13) \text{ MeV}$. It agrees with the BES measurement quite well within 1σ [8] and improves the precision by an order of magnitude. These measurements have a big impact on our knowledge about the χ_{c0} resonance parameters [4], and are expected to play a crucial role in our understanding of the strong force governing the $c\bar{c}$ system [39, 45]. A comparison of our results with other measurements as well as the PDG world average is shown in Fig. 2.

The decay BF's are measured to be

$$\mathcal{B}(\chi_{c0} \rightarrow K^+ K^-) = (6.36 \pm 0.02 \pm 0.08 \pm 0.13) \times 10^{-3},$$

$$\mathcal{B}(\chi_{c0} \rightarrow \pi^+ \pi^-) = (6.06 \pm 0.02 \pm 0.07 \pm 0.13) \times 10^{-3},$$

$$\mathcal{B}(\chi_{c2} \rightarrow K^+ K^-) = (1.22 \pm 0.01 \pm 0.02 \pm 0.03) \times 10^{-3},$$

$$\mathcal{B}(\chi_{c2} \rightarrow \pi^+ \pi^-) = (1.61 \pm 0.01 \pm 0.02 \pm 0.04) \times 10^{-3},$$

where the first uncertainties are statistical, the second systematic, and the third come from $\mathcal{B}[\psi(3686) \rightarrow \gamma \chi_{c0,c2}]$ [4]. These measurements agree with the CLEO-c result within 1σ [46], and improve the precision by more than threefold. Interestingly, the ratio of BF's $\mathcal{R} = \frac{\mathcal{B}(\chi_{c0} \rightarrow \pi^+ \pi^-)}{\mathcal{B}(\chi_{c0} \rightarrow K^+ K^-)} = (0.95 \pm 0.01 \pm 0.01)$ demonstrates no obvious ‘Chiral Suppression’ is observed for this 0^{++} system, which supports the theoretical analysis in Ref.

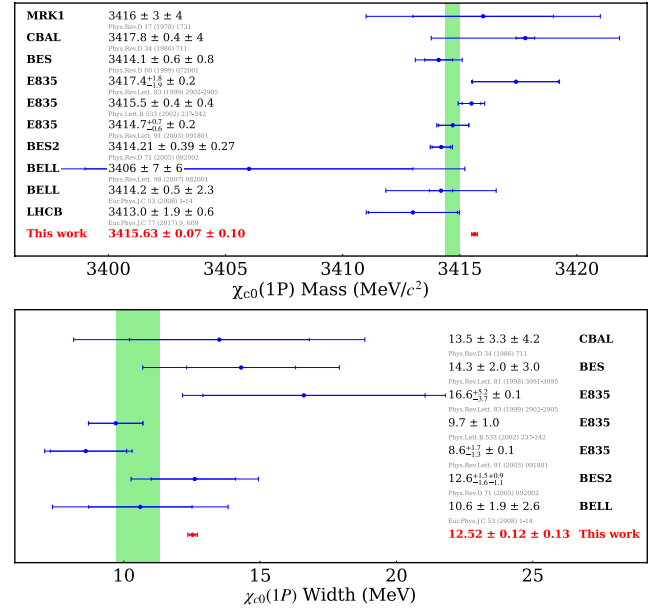


Fig. 2. (color online) Comparison of the χ_{c0} resonance parameters measurements. The light green bands represent the PDG world average [4].

[47, 48]. This behavior is also quite different from the case of the $f_0(1710)$ [19, 20], therefore challenging the scalar glueball interpretation of the $f_0(1710)$ state [21]. It implies $f_0(1710)$ might contain a substantial $s\bar{s}$ component, which aligns with the model calculations in Ref. [49, 50]. Combining our precisely measured $\mathcal{R}$ value, which constrains the glueball fraction in $f_0(1710)$, with future theoretical improvements will advance our understanding of QCD.

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