Nuclear Shadowing Effect in Photoproduction Process at LHC

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Abstract In the paper we give some results about nuclear shadowing of real photon at LHC. We show that shadowing grows strong with the increasing of photon energy E_{γ} . The CMS energy dependence of total cross sections of production of ρ , ω and φ in the process $\gamma + A \rightarrow V + A$ is also given. The results show that there is a critical energy point, above which the nuclear shadowing is strong enough to be observed.

Key words elastic photoproduction process, nuclear shadowing, vector mesons

Nuclear shadowing effect in deep-inelastic scattering off nuclei is a hot topic for the last two decades^[1]. The experimental result implies that the total $\sigma(\gamma^*A)$ on a nucleus (with mass number A) at small Bjorken x (x < 0.01) is less than A times the total cross section $\sigma_{tot}(\gamma^*N)$ on a nucleon. Many theoretical efforts have been devoted to understand this phenomenon quantitatively, among which a very intuitive picture arises in the rest frame of the nucleus, where shadowing may be understood in the following way: The virtual photon fluctuates into a hadronic state that interacts with the nucleus at it's surface and the nucleons inside have less chances to interact with the photon, thus the total cross section is less than expected naively. This idea leads to the vector meson dominance model. The fluctuation extends over a distance called coherence length

$$\lambda = \frac{2E_{\gamma}}{Q^2 + M_{\rm X}^2} \,, \tag{1}$$

where M_X is the invariant mass of the fluctuation, E_Y is the energy of the photon and Q^2 is the virtuality of the photon which is related to the size R_A of the nucleus by $Q^2 \le 1/R^2$. The shadowing correction is given by [2]

$$\sigma_{\text{tot}}^{\gamma^* A} = A \sigma_{\text{tot}}^{\gamma^* N} - A \langle T \rangle \int d^2 b \int dM_X^2 \frac{d^2 \sigma(\gamma^* N \to XN)}{dt dM_X^2} \bigg|_{t=0} F_A^2(\lambda, b), \tag{2}$$

where the nuclear form factor is

Received 8 June 1999

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$$F_{\rm A}^2(\lambda, b) = \frac{1}{A\langle T \rangle} \left| \int_{-\infty}^{+\infty} {\rm d}z \rho_{\rm A}(b, z) \exp({\rm i}z/\lambda) \right|^2, \tag{3}$$

$$\langle T \rangle = \frac{1}{A} \int d^2b T^2(b),$$
 (4)

where the nuclear thickness $T(b) = \int dz \rho_A(b,z)$ is the integral of the nuclear density over the direction of the incident photon and b is the impact parameter. We choose the nuclear density as the Gaussian $\rho_A(r) = A(\pi R_A^2)^{-3/2} \exp(-r^2/R_A^2)$. The radius of a nucleus is given approximately by $R_A = 1.2 A^{1/3}$, where A is the nucleon number.

From the above equations we obtain

$$\sigma_{\text{tot}}^{\gamma^* A} = A \sigma_{\text{tot}}^{\gamma^* N} \left[1 - \frac{2A^{1/3}}{a^2} \frac{1}{\sigma_{\text{tot}}^{\gamma^* N}} \int dM_X^2 \frac{d^2 \sigma(\gamma^* N \to XN)}{dt dM_X^2} \bigg|_{t=0} \exp\left(-\frac{a^2 A^{2/3}}{2\lambda^2} \right) \right], \tag{5}$$

where $a \simeq 1.2$ fm.

In the theory of lepton-nucleus interactions there is a close relation between nuclear shadowing and diffractive scattering which has been tested by E665 Collaboration^[3]. This means one can take the Regge theoretical diffractive result, the double differential cross section for the process $\gamma^* + N \rightarrow X + N$

$$\frac{\mathrm{d}^2 \sigma^{\mathrm{D}}(\gamma^* \mathrm{N} \to X \mathrm{N})}{\mathrm{d} t \mathrm{d} M_{\mathrm{X}}^2} \sim \left(\frac{1}{M_{\mathrm{X}}^2}\right)^{\alpha P(0)} (W^2)^{2\alpha P(0) - 2} e^{b|t|} \tag{6}$$

into Eq.(5) to get the shadowing result.

It is easy to extrapolate the above results to the real photonic shadowing phenomenon in the limit $Q^2 \to 0$. Keeping the real photon massless, shadowing still occurs via the above physical picture. The coherence length of hadronic states of mass M_{χ} , produced by a real photon of energy E_{γ} is

$$\lambda = \frac{2E_{\gamma}}{M_{\rm v}^2} \,. \tag{7}$$

We therefore expect that the total cross section $\sigma_{\rm tot}(\gamma A) < A\sigma_{\rm tot}(\gamma N)$. To discuss the photonuclear effects it is also useful to define the effective number of nucleons in the nucleus by

$$\frac{A_{\text{eff}}}{A} = \frac{\sigma(\gamma A)}{A\sigma(\gamma N)},$$
(8)

$$\frac{A_{\text{eff}}}{A} = 1 - \frac{2A^{1/3}}{a^2} \frac{1}{\sigma_{\text{tot}}^{\gamma N}} \int dM_X^2 \frac{d^2 \sigma^D(\gamma N \to XN)}{dt dM_X^2} \bigg|_{t=0} \exp\bigg(- \frac{a^2 A^{2/3}}{2\lambda^2} \bigg). \tag{9}$$

Using HEAR diffractive photoproduction results^[4] for the above equations, we obtain the shadowing ratio $\frac{A_{\rm eff}}{A}$ for Pb and Ca nuclei in the photonuclear process at LHC, which is shown in Fig. 1. In the LHC process $\gamma A \rightarrow XA$ the maximum energy of photon E_{γ} may arrive to 80GeV for Pb and 180GeV for Ca respectively. Fig. 1 shows that shadowing grows stronger for higher photon energy E_{γ} , eventually approaching some saturation value. This is due to the fact that the coherence length

govern scattering processes. This can be easily understand from Eq. (9), taking the limit $\lambda \rightarrow \infty$ one can obtain

$$\frac{\sigma(\gamma A)}{A\sigma(\gamma P)} = 1 - \frac{2A^{1/3}}{a^2} \frac{1}{\sigma(\gamma P)} \frac{d\sigma^{D}(\gamma P \to XP)}{dt} \bigg|_{t=0}.$$
(10)

It is also interesting to study elastic vector meson photoproduction in the processes $A + A \rightarrow V + A + A$, $(V = \rho, \omega, \phi)$ at LHC. The equivalent photon spectrum function^[5] is given by

$$n(E_{\gamma}) \approx \frac{2Z^2\alpha}{\pi E_{\gamma}} \ln\left(\frac{\gamma_1}{RE_{\gamma}}\right),$$
 (11)

where $R = b_{\min}(b_{\min})$ is the cut-off of impact). γ is Lorentz factor of nuclei. The

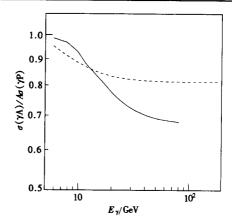


Fig. 1 The shadowing ratio for the absorption of real photons on nuclei as a function of photon energy E_{γ} , solid line for Pb and dashed line for Ca

production cross section of a photon fusion a parton in the nucleus in the collision of heavy-ion is given by

$$\sigma_{\text{tot}}(AA \to AAV) = \int dE_{\gamma} n(E_{\gamma}) \sigma_{\text{tot}}(\gamma A \to VA), \qquad (12)$$

$$\sigma_{\text{tot}}^{\gamma A} = A \sigma_{\text{tot}}^{\gamma P} \left[1 - \frac{2A^{1/3}}{a^2} \frac{1}{\sigma_{\text{tot}}^{\gamma P}} \frac{d\sigma^{D}(\gamma P \rightarrow VP)}{dt} \right|_{t=0} \exp \left(-\frac{a^2 A^{2/3}}{2\lambda^2} \right) , \qquad (13)$$

where

$$\lambda = \frac{2E_{\gamma}}{Q^2 + M_{\nu}^2} \,. \tag{14}$$

Using HEAR diffractive photoproduction results^[6] of vector mesons for the above equations, we obtain the total cross section of elastic production of ρ , ω and φ in the process $\gamma + A \rightarrow V + A$ which are shown in Fig. 2(a) is for the process $\gamma + Pb \rightarrow V + Pb$. When CMS energy of γ -Pb is below 240GeV the total cross section of ρ (the solid line in the figure) shows a very good shape like $\sigma(\gamma Pb) \sim A\sigma(\gamma P) \sim AW^{0.22}$, while W > 240GeV the shadowing effect becomes very strong, here the critical energy point W = 240GeV is correspond to $E_{\gamma} = 5.0$ GeV. So do that of ω and φ where the critical energy point are W = 292GeV, $E_{\gamma} = 7.2$ GeV and W = 339GeV, $E_{\gamma} = 9.7$ GeV. Fig. 2(b) is for the process $\gamma + Ca \rightarrow V + Ca$. Here we get the similar results as those in Fig. 2(a). W = 250GeV, $E_{\gamma} = 4.1$ GeV for φ and ω , W = 330GeV, $E_{\gamma} = 7.2$ GeV for φ .

In conclusion, we have given some results about nuclear shadowing of real phoon at LHC. We show that shadowing grows strong with the increasing of photon energy E_{γ} . The CMS energy dependence of total cross sections of elastic production of ρ , ω and φ in the process $\gamma + A \rightarrow V + A$ is also given. The results show that there is a "critical" energy point, above which the nuclear shadowing is strong enough to be observed. So we think that the phenomenology of high energy real photonic nuclear shadowing may be an interesting subject of LHC, which can be studied in detail.

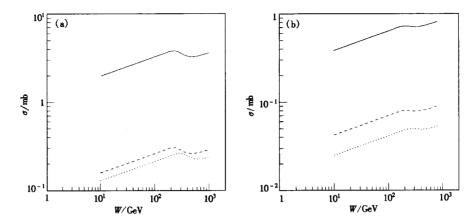


Fig. 2 (a) CMS energy distribution of total cross section of elastic photoproduction of ρ (solid line), ω (dashed line) and φ (dotted line) in γ + Pb→V + Pb processes.
(b) CMS energy distribution of total cross section of elastic photoproduction of ρ(solid line), ω (dashed line) and φ (dotted line) in γ + Ca→V + Ca processes

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LHC 光生过程中的核遮蔽效应

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摘要 给出了关于 LHC 实光子核遮蔽效应的一些结果.证明了遮蔽随光子能量 E_{γ} 的增加而变强.给出了反应过程 $\gamma + A \rightarrow V + A$ 中的 ρ , ω , φ 总截面对质心系能量的依赖性.结果表明,存在一个能量的临界点,在该点以上的核遮蔽强到足可以被测到.

关键词 弹性光生过程 核遮蔽 矢量介子

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